

**Final Examination [40 points], Monday, June 7, Spring 2010  
MATH 210 Calculus III, Section 01, Dr. Masayoshi Kaneda  
Department of Mathematical Sciences, Faculty of Science  
United Arab Emirates University**

**Name (Printed):**

**Student ID:**

**The quiz will be first graded out of 68 points, and then the score is converted to be out of 40 points.**

1. (Exercise 12.7.37, homework, covered in lab) [18 points] Find the absolute extrema of the function  $f(x, y) = x^2 + 3y - 3xy$  on the region bounded by  $y = x$ ,  $y = 0$ , and  $x = 2$ .

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2. (Exercise 13.1.55, homework) [7 points] Evaluate the iterated integral by first changing the order of integration.

$$\int_0^1 \int_y^1 3xe^{(x^3)} dx dy$$

3. (Exercise 13.2.17, homework, covered in lab) [10 points] Compute the volume of the solid lying in the first octant bounded by  $z = 1 - y^2$ ,  $x + y = 1$ , and three coordinate planes.

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4. (Example 13.3.4, covered in lecture, modified) [12 points] Evaluate the iterated integral.

$$\int_0^1 \int_0^{\sqrt{1-x^2}} x^2(x^2 + y^2)^2 dy dx$$

5. (Example 13.5.2, covered in lecture) [21 points] Evaluate  $\iiint_Q 6xy dV$ , where  $Q$  is the tetrahedron bounded by the planes  $x = 0$ ,  $y = 0$ ,  $z = 0$ , and  $2x + y + z = 4$ .