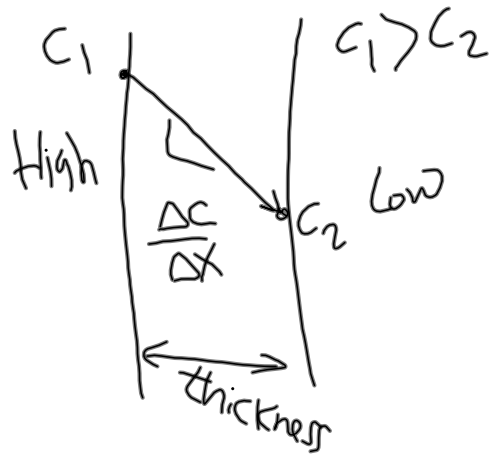


Diffusion



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Steady-State



Oct 5-12:10 PM

Q1

$$C_1, J$$

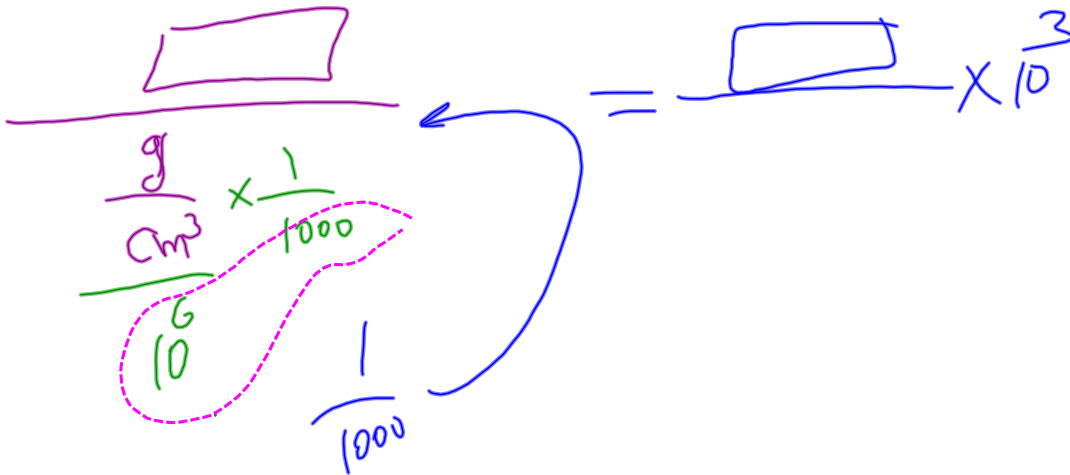
$$C_2, X$$

$$J = -D \frac{dc}{dx}$$

$$\frac{dc}{dx} \rightarrow C_2 - C_1$$

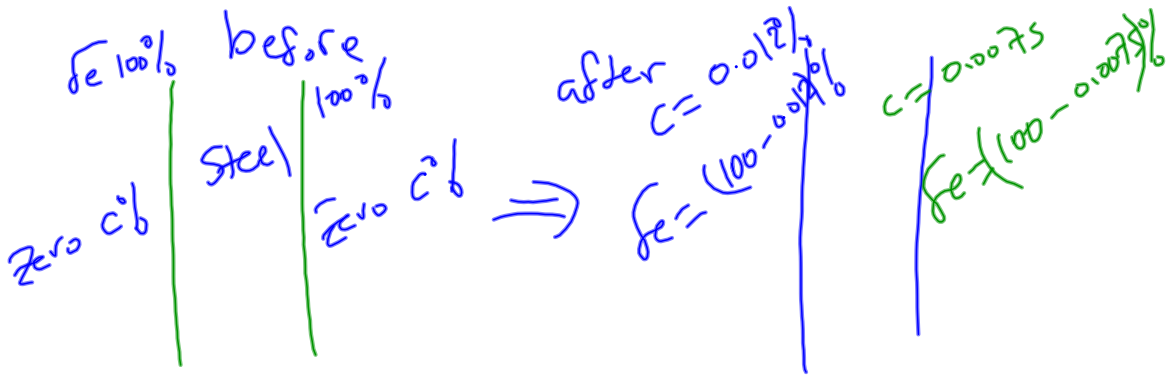
thickness (m)

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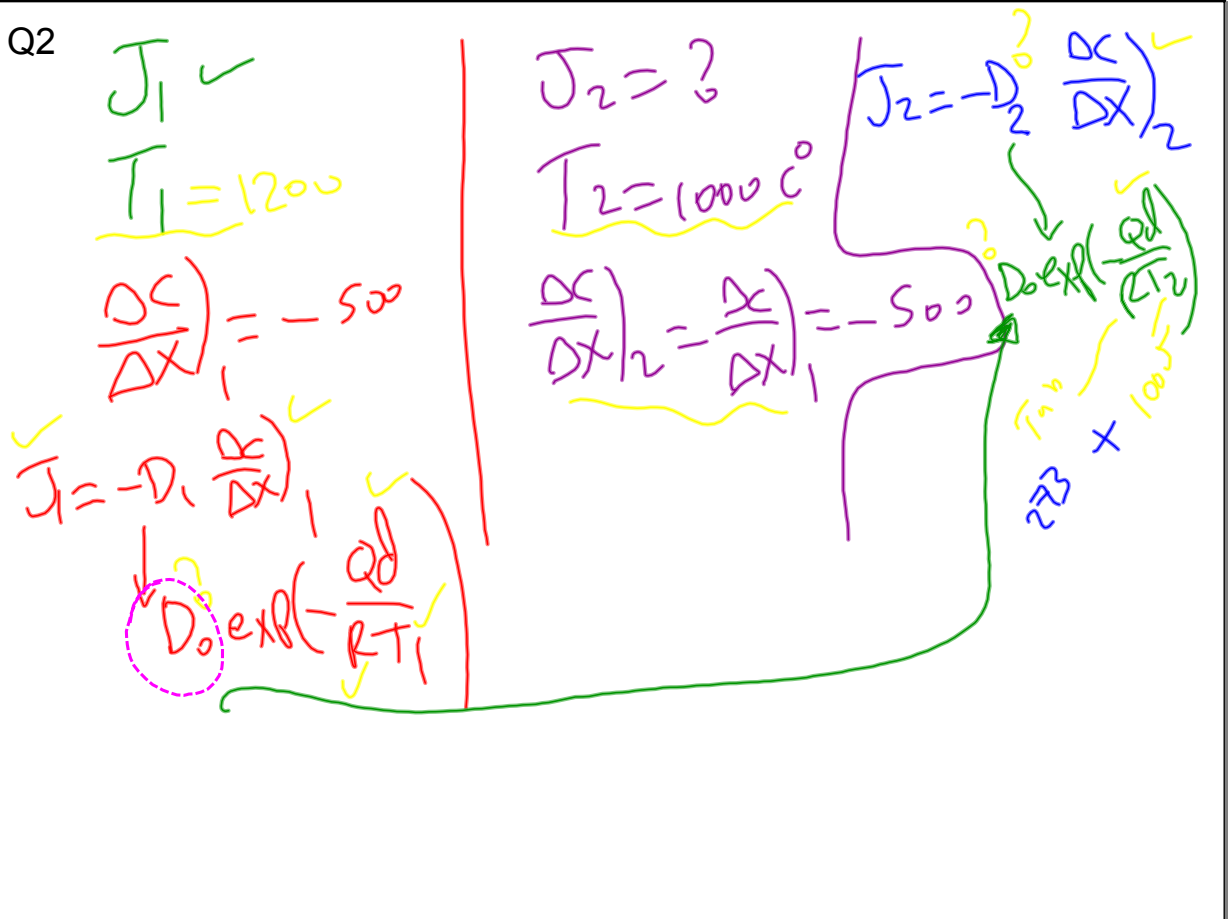
Oct 5-12:35 PM

Composition conversions (chapter 4)



Oct 5-12:32 PM

Q2



Oct 5-12:40 PM

Non-Steady State

Steady $C = f(x) \Rightarrow$ Linear
Non-stead $C = f(x, t)$

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Assumptions

- 1- $t=0, C=C_0$ (initial)
- 2- $t>0, C=C_s$ (surface)
- 3- C_x at any x at any time

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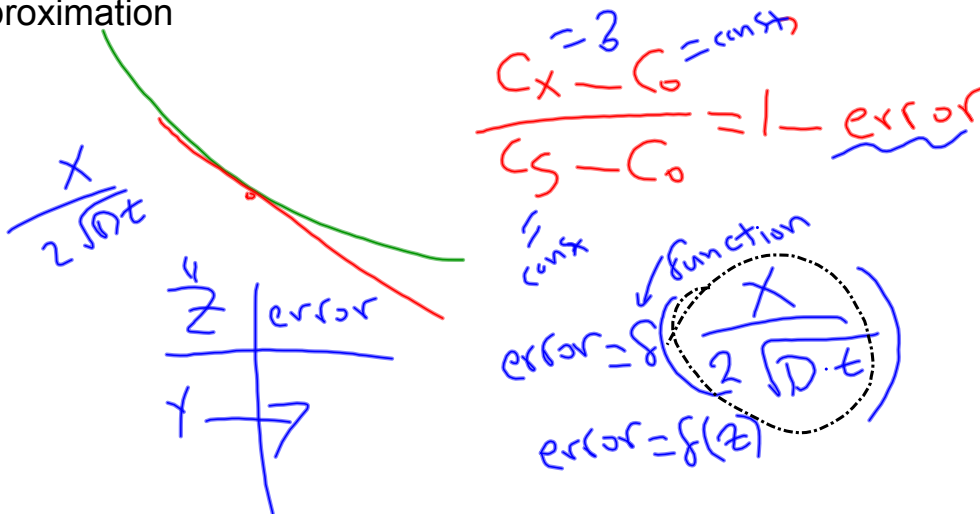
$$D = D_0 \exp\left(-\frac{Q_d}{R \cdot T}\right)$$

D_0 is a constant.
 R is the gas constant.
 T is temperature in Kelvin (K).
 Q_d is the activation energy.

D is used for steady and the non-steady cases

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Approximation



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Q3

$t_1 = 15 \text{ hr}$
 $x_1 = 2 \text{ mm}$
 $c_2 = 0.35\%$
 $t_2 = ?$
 $c_1 = 0.35\%$
 $x_2 = 6 \text{ mm}$

$\frac{c_x - c_0}{c_s - c_0} = 1 - \text{erf}(z)$
 $\text{error} = \text{const} = f(z)$
 $D = D_0 \exp\left(-\frac{Q_d}{RT}\right)$
 $\frac{x}{2\sqrt{D \cdot t}} = \text{const} \Rightarrow \frac{x_1}{2\sqrt{D_1 t_1}} = \frac{x_2}{2\sqrt{D_2 t_2}}$
 $\frac{x_1^2}{t_1} = \frac{x_2^2}{t_2}$
 $\frac{t_1}{t_2} = \left(\frac{x_1}{x_2}\right)^2$

time

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Q4 time

$\frac{c_x - c_0}{c_s - c_0} = 1 - \text{error}$
 $\text{error} = 1 - \frac{c_x - c_0}{c_s - c_0}$
 $z = \frac{x}{2\sqrt{D \cdot t}}$
 $D = D_0 \exp\left(-\frac{Q_d}{RT}\right)$

z | error

Table

Oct 5-1:16 PM

Q5 ✓

$$\frac{C_x - C_0}{C_s - C_0} = 1 - \text{error}$$

error = ✓

z	error
ⓧ	x

$$z = \frac{x}{2\sqrt{Dt}} = \frac{50}{2\sqrt{10 \times 10^{-6} \times 1000}} = 50$$

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