Keywords: Google PageRank Algorithm, PPI, Protein Complex, Essential Protein, ProRank Algorithm.

Abstract: The course of developing effective medical treatments is typically based on the identification of disease-triggering protein complexes. In this paper, we present ProRank+, an effective method for detecting protein complexes in protein interaction networks. By assuming that complexes may overlap, the method uses a ranking algorithm to order proteins based on their importance in the network. In addition, a novel merging procedure is introduced to refine the predicted complexes in terms of their members. The experimental studies and results showed that ProRank+ outperforms several state-of-the-art methods in terms of the number of correctly-detected protein complexes using numerous quality measures.

1 INTRODUCTION

Cellular functions are often executed through collaborations of protein groups referred to as protein complexes (Gavin et al., 2006). Accordingly, identifying protein complexes in protein interaction networks is an essential step towards understanding normal cellular processes as well as defining and treating possible diseases induced by their malfunctions. The biological methods employed for the detection of protein complexes often face drawbacks, mainly in high time and cost requirements. Therefore, many computational methods were designed in order to complement the experimental efforts by highlighting protein groups which could potentially delineate various cellular functions. In a computational context, a protein interaction network is usually modeled as an interaction graph in which vertices represent the proteins and edges represent their interactions. In this setting, it is generally assumed that protein complexes correspond to dense subgraphs within the graph. Among the recent methods, we herein highlight: Markov Clustering (MCL) (Dongen, 2000) which uses random walks in protein interaction networks, the molecular complex detection (MCODE) algorithm (Bader and Hogue, 2003) which identifies complexes as dense regions grown from highly-weighted vertices, the clustering based on maximal cliques (CMC) method (Guimei et al., 2004), the Affinity Propagation (AP) algorithm (Frey and Dueck, 2007), ClusterONE (Nepusz et al., 2012) which identifies protein complexes through clustering with overlapping neighborhood expansion, the restricted neighborhood search (RNSC) algorithm (King et al., 2004; Przulj et al., 2004), the RRW algorithm which generates complexes by using repeated random walks (Macropol et al., 2009), CFinder (Adamcsek et al., 2006) which is based on the clique percolation method. These methods, among several ones, showed relatively good performance in detecting protein complexes. However, by assuming that protein complexes correspond to dense subgraphs in the interaction network limits, the detection process is limited since it does not usually allow the identification of complexes with few members and/or few interactions. ProRank (Zaki et al., 2012a) is a recent method developed to detect protein complexes from protein interaction networks based on a protein ranking algorithm. When compared with previous methods, the experimental studies showed a good performance of the ProRank algorithm in terms of the number of detected protein complexes as well as precision, recall and accuracy levels. In spite of that, ProRank does not take into account possible overlaps among the detected complexes. In fact, a protein can exhibit many
functions by being part of different complexes (Hodgkin, 1998). Therefore, it is beneficial to reflect this fact when searching for protein complexes in interaction networks. Moreover, ProRank computes a similarity matrix consisting of the similarity scores among all the proteins in the interaction network. This step can be discarded since it is computationally-expensive and has a comparatively small effect on the final results (Zaki et al., 2012b). In this paper, we present ProRank+, an enhanced protein-complex detection algorithm which detects possibly-overlapping complexes. Additionally, the method includes a novel merging procedure, Merging by Cohesiveness, used to refine the detected protein complexes. In this setting, complexes are viewed as entities of highly-interconnected members that are well-separated from the rest of the interaction network. The experimental studies and results greatly favor our approach.

2 THE PRORANK+ METHOD

ProRank (Zaki et al., 2012a,b) is a recently-introduced method designed to detect protein complexes in protein interaction networks. It mainly consists of a protein ranking algorithm inspired by Google's PageRank algorithm (Bryan and Leise, 2006; Langville and Meyer, 2006; Ishii and Tempo, 2010) which quantifies and ranks web pages by their level of importance. Likewise, ProRank applies the same analogy on protein interaction networks to rank proteins and pinpoint the "essential" ones which play key roles in cellular processes. Those proteins are then considered as starting points to form the detected complexes. Five main steps outline the ProRank algorithm:

a. Pruning: removing unreliable interactions that could negatively affect the detection process using the AdjustCD method (Hon et al., 2006; Chua et al., 2008), a weighting scheme that iteratively calculates the reliability of protein interactions based on the topology of the interaction network and considers as unreliable those whose weights are less than a specified threshold.

b. Filtering: a protein interaction network usually contains noisy proteins which may belong to one of the following types: bridge proteins which have a disconnected subgraph of neighbors; fjord proteins whose neighbors have a small number of interactions among each other; and shore proteins which have at least one neighbor with significantly few interactions with other proteins. Proteins in the network are examined for possible belonging to these types.

c. Protein Similarity Calculating: Based on the assumption by which proteins belonging to the same complex most likely have evolutionary relationships, the similarity scores among all the proteins in the network are calculated using their pairwise alignment scores.

d. Protein Ranking: a ranking algorithm is used to rank proteins based on the number of interactions in which they participate and the similarity levels among them.

e. Complex Detection: protein complexes are detected using the spoke model. Essential proteins are considered by their decreasing ranking order and each of them is along with its neighbors form a protein complex. It is assumed here that every protein in the network can belong to one complex only.

A hypothetical protein interaction network consisting of 16 proteins (numbered from 1 to 16) and 4 complexes: Cmplx1 = {1,2,3,4} colored in blue, Cmplx2 = {4,5,6,7,16} colored in yellow, Cmplx3 = {8,9,10,16} colored in green, and Cmplx4 = {10,11,12,13,14} colored in red. A hypothetical protein interaction network is presented in Figure 1. The steps of the ProRank method when applied on this network are summarized in Table 1. For simplicity, all the interactions are considered reliable and the similarity among all the proteins is assumed to be uniform. Three complexes are detected: C1 = {6,4,5,7,16}, C2 = {14,10,11,12,13} and C3 = {1,2,3}. They correspond to essential proteins 6, 14 and 1 and their direct neighbors consecutively.
A protein can participate in multiple cellular functions by being part of several protein complexes (Hodgkin, 1998). For instance, among the 1189 proteins contained in the MIPS catalog of protein complexes (Mewes et al., 2004), 820 proteins (approx. 69%) belong to more than one complex. Similarly, among the 1279 covered by the SGD complex set (Hong et al., 2008), 332 proteins (approx. 26%) belong to multiple complexes. Hence, accounting for this biological fact would most likely increase the reliability of complex-detection algorithms. Accordingly, we start out from this notion to introduce ProRank+. For instance, we applied this notion on the network presented in Figure 1 knowing that only the complex-detection step is modified. Thus, the types and the ranking scores of the proteins remain the same since the steps used to generate them, including the ranking algorithm, are unchanged. Table 2 summarizes the iterations in this case.

The results of applying ProRank+ on the given hypothetical example uphold the improvement added by the overlap extension which could potentially lead to a more correct detection of protein complexes. However, it can be noticed that some of the detected complexes are generated more than once. This was anticipated. Actually, since all essential proteins are now seeds for forming protein complexes, the ones that share the same set of neighbors will produce identical copies of the same complex. In order to overcome this limitation and to further improve the quality of the predicted complexes, the algorithm is modified as follows:

### Table 1: Types, ranking scores, and assigned complexes given by the ProRank method applied on the protein interaction network presented in Figure 1.

<table>
<thead>
<tr>
<th>Protein</th>
<th>Type</th>
<th>Ranking</th>
<th>Complex</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>Essential</td>
<td>0.0625</td>
<td>C1</td>
</tr>
<tr>
<td>5</td>
<td>Essential</td>
<td>0.0625</td>
<td>C1</td>
</tr>
<tr>
<td>14</td>
<td>Essential</td>
<td>0.0596</td>
<td>C2</td>
</tr>
<tr>
<td>13</td>
<td>Essential</td>
<td>0.0596</td>
<td>C2</td>
</tr>
<tr>
<td>12</td>
<td>Essential</td>
<td>0.0596</td>
<td>C2</td>
</tr>
<tr>
<td>11</td>
<td>Essential</td>
<td>0.0596</td>
<td>C2</td>
</tr>
<tr>
<td>1</td>
<td>Essential</td>
<td>0.0539</td>
<td>C3</td>
</tr>
<tr>
<td>7</td>
<td>Essential</td>
<td>0.0478</td>
<td>C1</td>
</tr>
<tr>
<td>9</td>
<td>Essential</td>
<td>0.0468</td>
<td>-</td>
</tr>
<tr>
<td>8</td>
<td>Essential</td>
<td>0.0468</td>
<td>-</td>
</tr>
<tr>
<td>3</td>
<td>Essential</td>
<td>0.0368</td>
<td>C3</td>
</tr>
<tr>
<td>2</td>
<td>Essential</td>
<td>0.0368</td>
<td>C3</td>
</tr>
<tr>
<td>10</td>
<td>Fjord</td>
<td>0.1167</td>
<td>C2</td>
</tr>
<tr>
<td>4</td>
<td>Fjord</td>
<td>0.1124</td>
<td>C1</td>
</tr>
<tr>
<td>16</td>
<td>Fjord</td>
<td>0.1044</td>
<td>C1</td>
</tr>
<tr>
<td>15</td>
<td>Bridge</td>
<td>0.0338</td>
<td>-</td>
</tr>
</tbody>
</table>

### Table 2: The complex-detection iterations corresponding to the modified complex-detection step.

<table>
<thead>
<tr>
<th>Complex-Detection Iteration</th>
<th>Essential Protein</th>
<th>Complex</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>6</td>
<td>{6,4,5,7,16}</td>
</tr>
<tr>
<td>2</td>
<td>5</td>
<td>{5,4,6,7,16}</td>
</tr>
<tr>
<td>3</td>
<td>14</td>
<td>{14,10,11,12,13}</td>
</tr>
<tr>
<td>4</td>
<td>13</td>
<td>{13,10,11,12,14}</td>
</tr>
<tr>
<td>5</td>
<td>12</td>
<td>{12,10,11,13,14}</td>
</tr>
<tr>
<td>6</td>
<td>11</td>
<td>{11,10,12,13,14}</td>
</tr>
<tr>
<td>7</td>
<td>1</td>
<td>{1,2,3,4}</td>
</tr>
<tr>
<td>8</td>
<td>7</td>
<td>{7,5,6,16}</td>
</tr>
<tr>
<td>9</td>
<td>9</td>
<td>{9,8,10,16}</td>
</tr>
<tr>
<td>10</td>
<td>8</td>
<td>{8,9,10,16}</td>
</tr>
<tr>
<td>11</td>
<td>3</td>
<td>{3,1,4}</td>
</tr>
<tr>
<td>12</td>
<td>2</td>
<td>{2,1,4}</td>
</tr>
</tbody>
</table>

a. The set of detected complexes is filtered in such a way to remove duplicates generated due to the added overlap supposition.

b. Next, a merging procedure referred to as **Merging by Cohesiveness**, is applied in the direction of exploring more variations of the detected complexes. All the produced complexes are matched against each other for possible merging. Two entities, $C_1$ and $C_2$, whose percentage of overlapping essential proteins is above a merging threshold, *merging threshold*, are merged along with their interconnections to form a larger complex $C$. Then, the process adopts the cohesiveness measure introduced in (Nepusz et al., 2012) to assess the quality of the resulting complex and its iteratively-extended variants defined hereafter. The cohesiveness of a complex $C$ is given by equation (1):

$$\text{Cohesive}(C) = \frac{w_{\text{in}}(C)}{w_{\text{in}}(C) + w_{\text{out}}(C) + p} \quad (1)$$

where $w_{\text{in}}(C)$ is the sum of the weights of edges that are entirely contained in $C$, $w_{\text{out}}(C)$ is the sum of the weights of edges that connect the proteins belonging to $C$ to the rest of the network, and $p$ is a penalty term reflecting uncertainties in the protein interaction network.

A protein complex is viewed as an entity with strongly-interconnected members that is well-separated from the rest of the network. For each protein, *prot*, contained in $C$, the set of its neighbors, $N_{\text{prot}}$, is formed. Then, for each neighbor protein, *prot*, in $N_{\text{prot}}$, the complex $C' = C \cup \{n_{\text{prot}}\}$ is constructed. And, if the cohesiveness of $C'$ is greater or equal to the cohesiveness of $C$, $n_{\text{prot}}$ is added to $C$. The final complex is added to the final list of detected complexes.
complexes. The pseudocode of merging two complexes is presented in Table 3.

Table 3: Merging by Cohesiveness Algorithm

Merge_by_Cohesiveness \((C1, C2, merging_threshold)\)

\[\begin{align*}
\text{ep1} &= \text{(set of essential proteins in C1)} \\
\text{ep2} &= \text{(set of essential proteins in C2)} \\
\text{if size(ep1) > size(ep2) then} & \quad \text{larger_set = ep1} \\
\text{else} & \quad \text{larger_set = ep2} \\
\text{end if} \\
\text{ep} &= \text{ep1} \cup \text{ep2} \\
\text{if size(ep) > size(larger_set) * merging_threshold then} & \quad \text{C} = \text{C1} \cup \text{C2} \\
\text{for prot in C} & \quad \text{N_prot} = \text{(set of neighbors of prot)} \\
\text{for n_prot in N_prot do} & \quad \text{C'} = \text{C} \cup \{n_prot\} \\
\text{if Cohesive(C') \geq Cohesive(C) then} & \quad \text{C} = \text{C} \cup \{n_prot\} \\
\text{end if} \\
\text{end for} \\
\text{end if}
\end{align*}\]

3 EXPERIMENTS AND RESULTS

3.1 Datasets and Evaluation Criteria

ProRank+ was tested on five large-scale protein-protein interaction datasets associated to the yeast microorganism. Four of the datasets consist of weighted protein interactions, they are: Collins (Collins et al., 2007), Krogan core and Krogan extended (Krogan et al., 2006), and Gavin (Gavin et al., 2006). The fifth dataset, BioGRID (Stark et al., 2006), contains unweighted interactions. The set of predicted complexes was matched against the MIPS catalog of protein complexes (Mewes et al., 2000). The datasets and the reference set of complexes were used to evaluate the ClusterONE method and to compare its performance with other approaches.

We also adopted the same quality scores applied in (Nepusz et al., 2012) to assess the quality of our algorithm. It is important to note that in their study, the parameters of the compared algorithms were optimized in such a way to produce best possible outcomes. The quality scores cover: (a) the number of complexes in the reference catalog that are matched with at least one of the predicted complexes with an overlap score, \(w\), greater than 0.25; (b) the clustering-wise sensitivity \((S_n)\) and (c) the clustering-wise positive predictive value \((PPV)\) which were originally introduced in (Brohée and van Helden, 2006) to calculate the matching quality, mainly in terms of the correctly-matched protein members among the detected complexes; (d) the geometric accuracy \((Acc)\) which is the geometric mean of \(S_n\) and \(PPV\); and (e) the maximum matching ratio \((MMR)\) which reflects how accurately the predicted complexes represent the reference complexes by dividing the total weight of the maximum matching by the number of reference complexes. Given \(m\) predicted complexes and \(n\) references complexes, the corresponding formulae are given by the following equations where \(t_{ij}\) represents the number of proteins that are found in both predicted complex \(m\) and reference complex \(n\).

\[
w(A, B) = \frac{|A \cap B|^2}{|A||B|} \quad (2)
\]

\[
S_n = \frac{\sum_{i=1}^{n} \max_{j=1}^{m} t_{ij}}{\sum_{j=1}^{n} n_j} \quad (3)
\]

\[
PPV = \frac{\sum_{j=1}^{n} \max_{i=1}^{m} t_{ij}}{\sum_{i=1}^{m} \sum_{j=1}^{n} t_{ij}} \quad (4)
\]

\[
Acc = \sqrt{S_n \times PPV} \quad (5)
\]

3.2 Experimental Settings of ProRank+

The steps of applying and testing ProRank+ on a given dataset, \(D\), and their experimental settings are:

a. Pruning: removing unreliable protein interactions from \(D\) using the AdjustCD method (Hon et al., 2006; Chua et al., 2008). We experimentally set the threshold to 0.2 for weighted datasets and to 0.45 for unweighted datasets.

b. Filtering: identifying bridge, fjord, and shore proteins which could add noise to the network, as defined in (Zaki et al., 2012a).

c. Protein Ranking: a ranking algorithm, analogous to the PageRank algorithm, is used to order the proteins.

d. Complex Detection: all the essential proteins, i.e. not assigned to any of the types in step b, are seeds based on which detected complexes are formed using the spoke model. Here, a protein can belong to more than one complex.
e. Pre-processing: The set of predicted complexes is filtered to remove possible duplicates generated due to the overlap supposition.

f. Merging by Cohesiveness: Two detected complexes whose overlap is above a merging threshold of 75% are merged. The subsequent complex is iteratively extended based on the introduced merging procedure.

g. Post-processing: the refined set of predicted complexes is finally filtered to remove possibly replicated copies of complexes.

3.3 Comparison with Other Methods

The performance of ProRank+ was then compared to other methods, applied on the same datasets and evaluated based on the same quality scores. These methods include ProRank (Zaki et al., 2012a) to highlight the attained improvement, MCL (Dongen, 2000), MCODE (Bader and Hogue, 2003), CMC (Guimei et al., 2004), AP algorithm (Frey and Dueck, 2007), ClusterONE (Nepusz et al., 2012), RNCS (King et al., 2004), RRW (Macropol et al., 2009), and CFinder (Adamcsek et al., 2006). The corresponding results scored by these approaches (Nepusz et al., 2012) and those scored by ProRank+ are displayed in Figures 2 and 3. Note that not all the algorithms can be applied to unweighted datasets which explains the fewer methods that were applied on the BioGRID dataset.

The experimental results show that ProRank+ was able to detect a higher number of protein complexes when matched with the reference set. ProRank+ achieved higher clustering-wise sensitivity ($S_n$), geometric accuracy ($Acc$) and maximum matching ratio ($MMR$) for all the considered datasets. However, it could not surpass the clustering-wise positive predictive value ($PPV$) of ProRank which was the highest for all datasets. This can be justified by the fact that $PPV$ tends to be lower when the overlaps among the detected complexes are substantial. $PPV$ values may not always reflect the competence of a certain method and the geometric accuracy ($Acc$) can be negatively affected by the predicted complexes that do not match any of the reference complexes. Accordingly, the $MMR$ measure (Nepusz et al., 2012) was introduced to overcome such limitations by dividing the total weight of the maximum matching with the number of reference complexes. The $MMR$ values achieved by ProRank+ are in the favor of the proposed algorithm.

4 CONCLUSION

In this paper, we presented ProRank+, an effective method for detecting overlapping protein complexes in protein interaction networks. A ranking algorithm is used to identify key proteins in the network and a merging procedure is introduced in the direction of refining the detected complexes. When tested on weighted and unweighted datasets, ProRank+ was able to detect more complexes than several state-of-the-art methods with higher quality scores. As future
work, we plan to test the method on various biological networks. In addition, we look to extend the approach in such a way to reflect the dynamic nature of protein interaction networks.

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